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# Comparison of the accumulation of fibre breaks occurring in a unidirectional carbon/epoxy composite identified in a multi-scale micro-mechanical model with that of experimental observations using high resolution computed tomography

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## ABSTRACT

A model to predict fibre break accumulation that takes into account all physical phenomena at the origin of the fibre break (i.e. the random nature, stress transfer due to breaks, fibre debonding and viscosity of the matrix) shows clearly that the failure of a unidirectional composite structure results in the formation of random fibre breaks which at higher loads coalesce into clusters of broken fibres.

The object of the study is to experimentally confirm this scenario. Many techniques exist to detect the failure of carbon fibre composites, however none of them offer a resolution that allows this goal to be achieved in a non-destructive manner and in three dimensions.

High resolution computed tomography has been used to confirm the scenario modelled. A sample was tested and observed in-situ at the European Synchrotron Research Facilities, ESRF, Grenoble. All fibre breaks arising in the vicinity of the final rupture of a unidirectional composite have been detected and the formation of clusters can be observed.

**MOTS-CLES :** high resolution computed tomography, fibre break, multi-scale modelling, unidirectional composite, micromechanics.

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## 1 Introduction

Many micromechanical theories exist to predict the failure of unidirectional composites. In tension, the failure of fibres is the critical damage mechanism, since the strength of an axially loaded unidirectional composite is dominated by the strength of the fibres. These simulations tend to include the statistical nature of fibre [1], calculation of the stress transfer coefficient around a fibre break [2] [3] [4] and coalescence of broken fibres into a critical cluster size resulting in final failure [5].

Experimental work to confirm the underpinning assumptions made in these theories however is limited and hence the true validity of the work has not yet been fully determined. The microscopic structure and complex nature of the failure process of composite laminates is difficult to characterise entirely. Previous work uses methods such as microscopy and acoustic emission sensing, to capture damage initiation and progression found in loaded composite structures. These methods however are limited. Microscopy is typically time consuming, with resultant images yielding a 2D representation of 3D processes [6]. Whilst offering good in-situ sensing, acoustic emission offers poor spatial resolution (in the order of mm) with potential ambiguity in interpretation.

High resolution computed tomography, CT, is gaining interest as an ideal tool for material mechanics studies [7]. It is a non-invasive method and provides 3D images in the micrometer and sub-micrometer range, of internal characteristics of materials and structures. CT can also be identified with what we are calling a data rich mechanics approach, where huge amounts of information of the micromechanical structure and behaviour can be identified in a relatively short space of time, depending of the equipment used, anything between a few minutes and an hour can yield two thousand 2D projections.

In the present work, high-resolution synchrotron radiation CT results have been obtained for carbon/epoxy  $[90^\circ/0^\circ]_s$  composite laminates subject to in-situ loading to failure. Due to the failure process, the data from

these samples can be used to compare with a unidirectional laminate. It can be seen in the results that matrix damage occurs in advance to fibre breaks and in fact decouples the  $90^\circ$  plies from the  $0^\circ$  plies. The fibre breaks then occur at higher loads in only the  $0^\circ$  plies.

The images enable individual fibres breaks to be identified and quantified. Providing a data set for existing predictive models to be compared and validated. The results give a unique physical insight into the failure process and enables the critical cluster size of fibre breaks to be identified.

## 2 Experimentation

Laminated  $[0^\circ/90^\circ]_s$  T700 aerospace grade carbon fibre pre-preg specimens were provided by Airbus and prepared by Wright *et al.* [8] for tensile loading. The double edge notches were machined using an abrasive waterjet to the geometry shown in Figure 1. The notched samples were used to ensure all damage mechanisms close to final failure could be captured. A sparse population of small aluminium particles ( $\approx 4\mu m$ ) were embedded into the laminates for fiducial markers.

A screw driven load frame, Figure 2 was used to load the samples in situ to failure. The samples were taken to incremental loads up to final failure. At each load step the samples were imaged at ID19 beamline at the European Synchrotron Radiation Facilities (ESRF) in Grenoble.

ID19 beamline routinely achieves resolutions of  $300nm$  and with specialised optics can achieve even high resolutions. The optics used in this study enabled a voxel resolution of  $1.4\mu m$  to be achieved. The coherent beam available from the synchrotron makes it possible for phase contrast imaging to be used, so an edge detection method can be exploited. This enables a crack opening of  $1/10$ th of the voxel size to be distinguishable and assists in finding small features such as fibre breaks.

High resolution is achieved via the high beam flux falling on a very high resolution detector system. In this experiment a FReLoN (Fast Read-out, Low Noise) detector attached to a  $2048 \times 2048$  pixel CCD camera was used. In comparison to conventional micro focus CT this enables relatively short exposure times (approximately 5 minutes a scan), so scans take a matter of minutes rather than hours. The detector measures the intensity distribution of the X-ray beam transmitted through the sample, which is proportional to the material density and also carries an energy dependence that is a function of the material composition [9]. The X-ray absorption is represented by corresponding grey scales and thus material and features such as cracks, voids and fibre breaks can be distinguished via a characteristic grey scale level shown in Figure 3. The result of the phase contrast imaging can also be seen in Figure 3, as black and white fringes surrounding the voids. Further details of the imaging setup can be found at [8].

The data was reconstructed using ESRF in-house software and the resulting 3D volumes were analysed using the software VG studio to segment and highlight regions of interest, such as cracks and fibre breaks, to present 3D images of the data.

Figure 4 shows the location in which the sample has been analysed and identifies the ply layup on a 3D reconstructed volume. The in-situ loading enables the damage progression to be identified up to failure, where Figure 5 shows the crack propagation in the same sample taken up to failure at 10% increments of the ultimate tensile strength, UTS. The transverse ply cracks occur early on in loading at 30% of the UTS. Further loading induces  $0^\circ$  splits which are then followed by delaminations.

Analysis of the in-situ samples shows the matrix cracking occurs in advance to fibre breaks and decouples the  $90^\circ$  plies from the  $0^\circ$  plies. There is no correlation between the fibre breaks and the matrix cracking and therefore the fibre breaks are the dominant damage mechanism.

The 3D capabilities of the CT imaging enables all fibre breaks to be identified in the sample through out the whole imaged volume. Figure 6 shows fibre breaks in exactly the same sample at two load increments. The same locations can be found in both samples using the marker particles. It is possible to see the accumulation of fibre breaks occurring with increasing load. Figure 7 shows a graph of the accumulation fibre breaks occurring in the samples with increasing load. The results show a distinct acceleration of fibre breaks occurring in the last 90% of loading.

It has also been possible to capture the growth of fibre clusters. Table 1 shows the cluster formation with increasing load. At 94% of the failure load 3 large clusters were found, consisting of 6, 8 and 12 neighbouring fibres. The largest of which can be seen in Figure 8. Where it is possible to view the clusters at all orientations and in 3 dimensions.

### 3 Modelling the phenomenon of fibre breakage and the comparison with experimental observations obtained by CT

The failure of unidirectional composite specimens has been studied for many years, with both analytical and statistical approaches being adopted, however few numerical models have been developed which take into account the viscoelastic behavior of the matrix. The following works can be cited, for example : Rosen [1], Cox [10], Zweben [11], Hedgepeth [3], Ochiai *et al.* [12], Goree and Gross [13], Harlow and Phoenix [2] [14], Scop and Argon [15] [16], Kong [17], Batdorf [5] [18], Nedele and Wisnom [19] [20], Hedgepeth and Van Dyke [4], Baxevanakis [21], Landis *et al.* [22] [23], Phoenix *et al.* [24] [25], Wisnom [26], Van Den Heuvel *et al.* [27] [28], Lipschitz and Rotem [29], Lagoudas *et al.* [30], Beyerlein *et al.* [31].

In this work, the phenomenon of fiber breakages in a unidirectional composite is studied at a microscopic scale, where the fibres and matrix are considered to be homogeneous materials.

The works of Blassiau *et al.* [32] [33] [34] [35] and those of Baxevanakis [21] initially identified the microstructure of the representative volume element (RVE) of the healthy material (i.e., not damaged and with out fibre breaks) symbolized by the cell called CS32, which contains 32 fibres.

At the microscopic scale a model of the phenomenon of fibre breakages and its consequences was constructed [32] [33] [34] [35] that takes into account :

- the random and inhomogenous nature of failure strength along the fibre axis. The variation of the Weibull modulus when only a small population, compared to a much larger population which leads to a deterministic value of the modulus, is considered, has also been taken into account [36];
- the number of broken fibres in the RVE through five states that allow damage to move from healthy microstructure to totally damaged. These five states of damage are symbolized by the representative cell of their RVE. These cells are named : C32, C16, C8, C4, C2. They contain  $N = 1, 2, 4, 8, 16$  broken fibres respectively among the 32 fibres present in the CS32 cell;
- axial stress transfer from broken fibres to intact fibres;
- axial stress transfer induced by the debonding of the fibre/matrix interface around the fibre break;
- axial stress transfer induced by the viscoelastic behavior of the matrix (assumed linear).

The simulations have been carried out by the Finite Element Method (Figure 9) employing the Zebulon code developed at the Mines Paristech using a simplified  $FE^2$  multiscale process [37]. There is good correlation between the observations and simulations. In addition, the simulations show that close to the final fracture of the sample, the fibre breaks no longer appear at random but group to form clusters which indicate the beginning of (unstable) rupture of the sample [37].

### 4 Conclusion

A notched  $[90^\circ/0^\circ]_s$  laminate has been used to gather a data set of damage mechanisms that occur in-situ loading to failure. Matrix crack formation occurs in the  $90^\circ$  plies prior to fibre breakages. As the load is increased the  $90^\circ$  plies become decoupled from the  $0^\circ$  plies and no relationship has been found between the matrix cracks and fibre breaks. Therefore it is evident that this sample layup can be used to inform a unidirectional model as to exact fibre break numbers, location and spatial distribution.

The accumulation of fibre breaks with load can be captured, where an acceleration of fibre breaks occurs beyond 90% of the failure load. The formation of fibre clusters is also identified, where the largest cluster was found to be 12 neighbouring fibre breaks at 94% of the failure load.

The data that can be extracted from these samples using the techniques included in this paper can be used with confidence; all fibre breaks and other damage mechanisms are easily distinguished and segmentable. Highly detailed quantification of material characteristics and failure mechanisms found in composite structures can be identified, which can then be used to inform and validate predictive modelling methods.

The fibre breaks observed by CT appear in an identical manner to the modelling predictions : in a state close to the ultimate failure of the sample, the fibre breaks no longer appear at random but group together to form clusters. This validates the relevance of the model and the assumptions with which it was built. Intralaminar cracks are also highlighted in the CT observations. They are not currently taken into account. However, it is highly likely that if these effects are taken into account the agreement between experiment (Figure 7) and model would be even closer. In fact, the intralaminar cracks that appear in the  $\pm 90^\circ$  layers will degrade the properties of the plies and hence increase the stress of the  $\pm 0^\circ$  plies : the fibre breaks will then occur earlier and faster.

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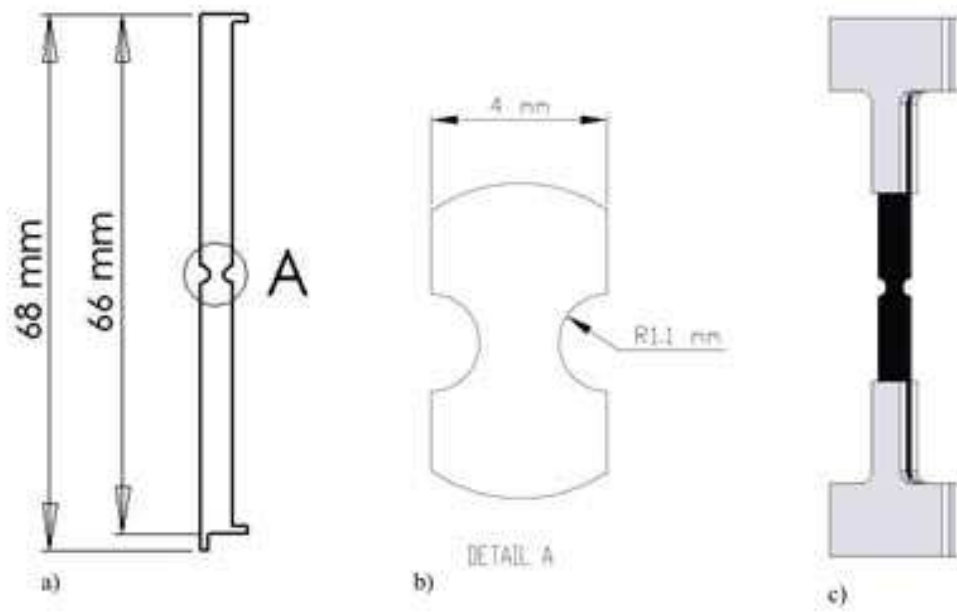


FIG. 1 – Notched sample specimen, a) and b) dimensions of the sample, c) illustration of end tabs used to grip during load.

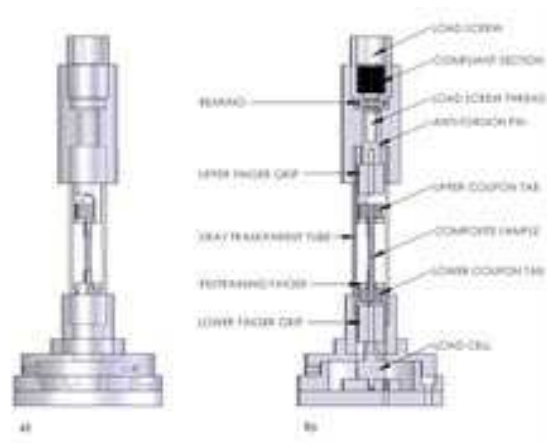


FIG. 2 – Screw driven loading device.

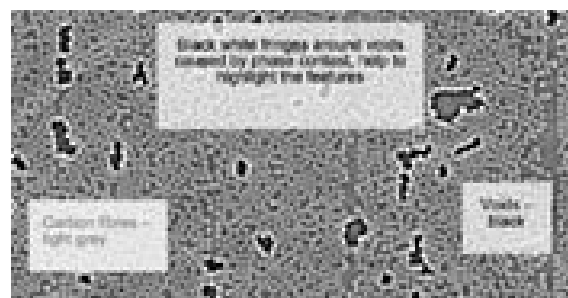


FIG. 3 – Example of absorption and phase contrast imaging.

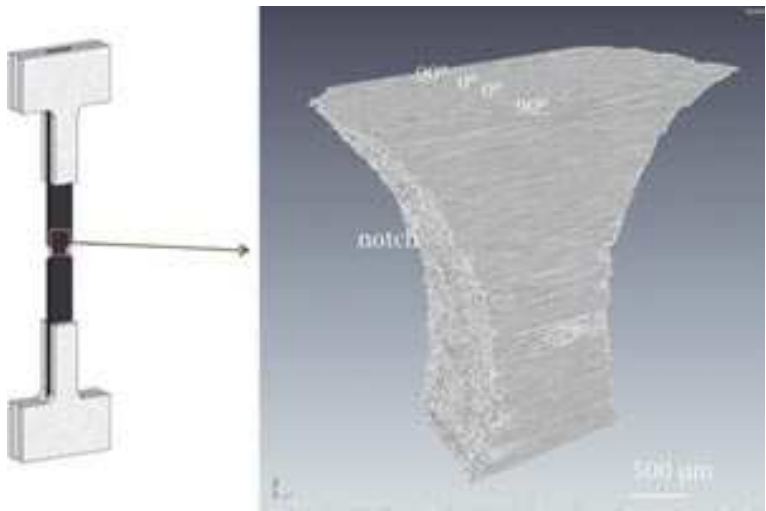


FIG. 4 – 3D reconstruction of notched sample.

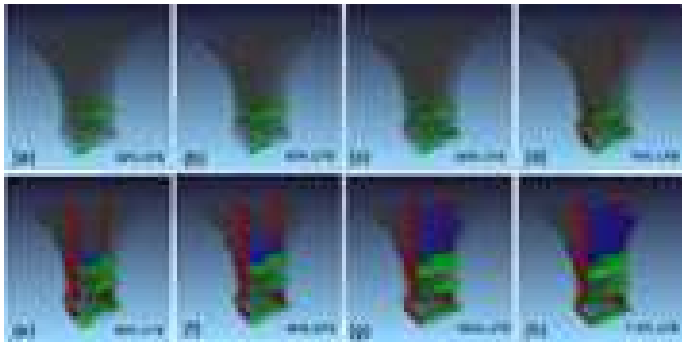


FIG. 5 – In-situ loading of sample. Composite made partially transparent. Transverse ply cracks in green, 0° splits in red and delamination in blue.

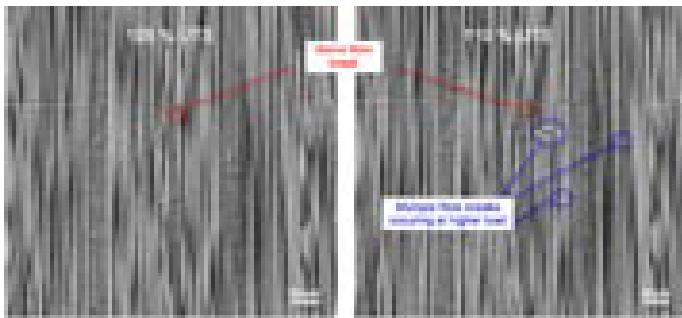


FIG. 6 – Fibre break accumulation in the same sample at different load increments.



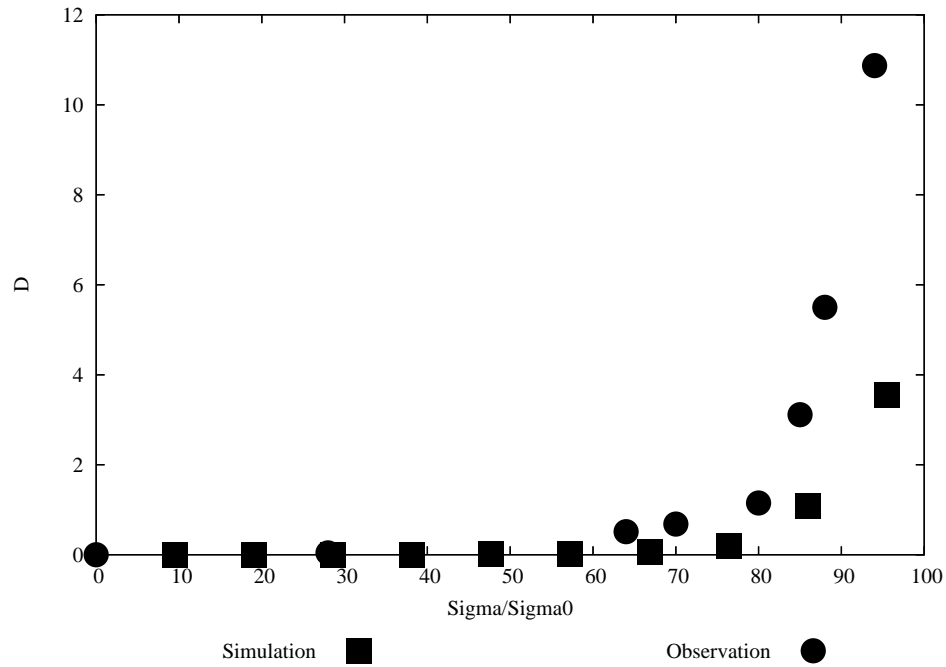


FIG. 7 – Density of fibre breaks ( $D$ ,  $nb/mm^3$ ) versus the increasing load ( $\Sigma/\Sigma_0$ ,  $\Sigma_0 = \text{UTS}$ ). Comparison between observation and simulation.

Numbers of cluster / Load (% of UTS)	0	28	64	70	80	85	88	94
1plet	0	1	6	10	15	58	98	151
2plet			3	3	6	6	9	13
3plet						1	3	7
4plet							1	3
5plet								
6plet								2
7plet								
8plet								1
9plet								
10plet								
11plet								
12plet								1

TAB. 1 – Fibre break cluster formation with increasing load.

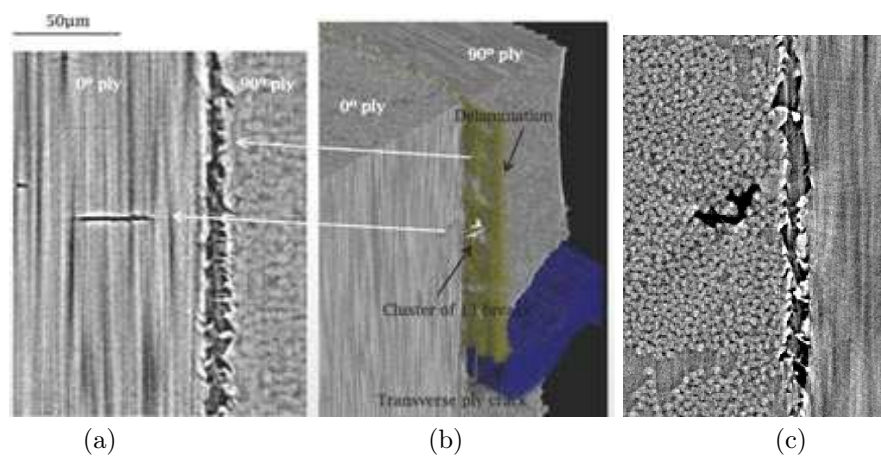


FIG. 8 – Fibre break identification, a) view of cluster aligned with fibres, b) 3D view, part of composite made transparent to reveal cluster, c) view of cluster face onto fibres.

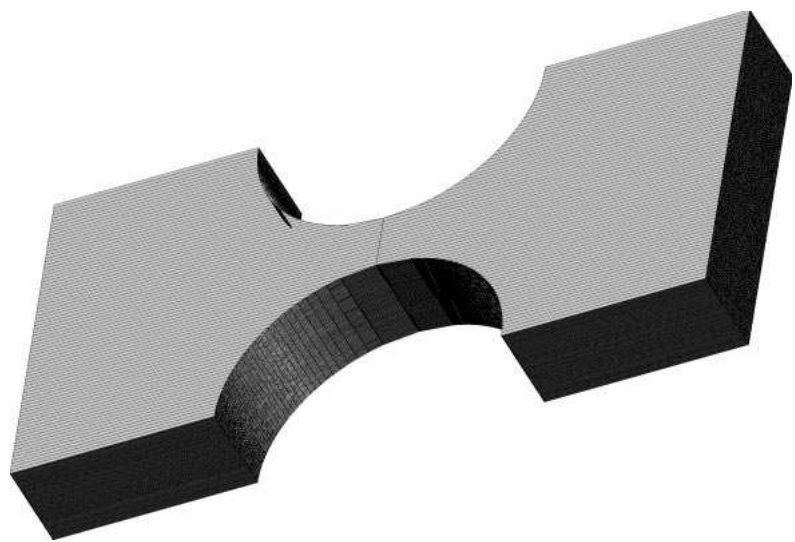


FIG. 9 – Mesh of the notched specimen.